UNIT OF STUDY

Title: Counting Techniques Subject/Course: Algebraic Connections Length: 10 days Topic: CS 1 unit 1 Grade: 12th **Designer:** Prado **UNIT GOALS AND EXPECTATIONS IMPORTANT CONCEPTS/UNDERSTANDINGS: ESSENTIAL QUESTIONS:** ◆ There is more than one way to count events How do I draw a tree diagram? ◆ Counting Techniques can save a lot of time What is the fundamental Counting Principle? ◆ Tree diagramming can make choice clearer ♦ When is an event independent or dependent? ♦ Solve permutations and combinations and relate ♦ When is a problem a permutation? them to real-life situations ♦ When is a permutation with repetition and without repetition? When is a problem a combination? STUDENT LEARNING EXPECTATIONS: PS.1AC.1 Apply counting techniques to determine the number of outcomes, tree diagram, fundamental Counting Principle, permutations (with and without repetition), and combinations SPECIFIC PROCEDURAL KNOWLEDGE – What I need to do SPECIFIC DECLARATIVE KNOWLEDGE - What I know Draw a tree diagram Explain vocabulary words: tree diagram, Solve a problem using the fundamental Counting fundamental Counting Principle, independent Principle events, dependent events, factorial, permutation, Solve a factorial combination ♦ Identify a tree diagram Add, subtract, multiply and divide factorials ◆ Find the value of a permutation ◆ Apply fundamental Counting Principle to problems Find the value of a combination ◆ Identify an independent event Reduce a fractional factorial expression Identify a dependent event Identify a factorial Rewrite a product of consecutive integer factors as a fractional factorial expression ◆ Identify a permutation Identify a combination

UNIT ASSESSMENTS

(Include tasks related to Dimensions 3 and 4 and Bloom's Taxonomy)

Traditional Assessments:

- ◆ Unit 1 Assessment
- ♦ Vocabulary Quiz
- ♦ Unit 1 Quizzes

Other Evidence of Learning:

- Homework
- Class work
- **Getting Started Problems**

ACTIVITIES AND LEARNING EXPERIENCES

Solving Problems using a Tree diagram

- S will learn vocabulary using the 4-step vocabulary process (tree diagram)
- ◆ S will do Getting Started activity sheet
- ◆ S will do hands-on activity creating sandwiches
- ◆ T will model tree diagramming and relate to sandwich activity
- ◆ S will do in-class worksheet on tree diagramming
- ◆ T will go over worksheet

Solving Problems using the Fundamental Counting Principle

- ♦ S will learn vocabulary: fundamental Counting Principle, independent events, and dependent events
- ♦ S will do hands-on activity creating outfits
- ♦ S will watch a short video on permutations done by the Boston Red Sox on Smartboard
- ◆ T will model fundamental Counting Principle (independent and dependent events), relate to outfits activity and how to use calculators
- ◆ S will do in-class worksheet on fundamental Counting Principle
- ◆ T will go over worksheet and assign homework

How to write and Solve Factorials

- ◆ S will learn vocabulary: factorial
- ◆ S will do Getting Started activity sheet
- ♦ T will model how a factorial is written, its notation, and how to use calculators to solve
- ♦ S will do worksheet on only writing out factorials and notation, not
- ◆ T will go over how to write worksheet
- ◆ T will model how a factorial is solved
- ◆ S will do worksheet on notation, writing, and solving factorials
- ◆ T will go over worksheet and assign homework

Adding, Subtracting and Multiplying Factorials

- ◆ S will do Getting Started activity sheet
- ◆ T will model how to add and subtract factorials (with proper notation) and how to use calculators to solve
- ◆ S will do worksheet on notation, writing out, adding and subtracting factorials
- ◆ T will go over adding and subtracting factorials worksheet

4-step vocabulary sheets

Resources

- Getting Started problems
- Sandwich bags with pieces of sandwich to create different sandwiches with one type of bread
- Tree diagramming worksheet
- Sandwich bags with pieces of clothing to create different outfits with different number of pants and shirts
- Fundamental Counting Principle worksheet
- ◆ Short video on permutations from www.teachertube.com
- Smartboard
- Calculators
- Getting Started problems
- Writing Factorial worksheet
- Solving Factorial worksheet
- Calculators

- Getting Started problems
- Adding and Subtracting factorials worksheet
- Multiplying factorials worksheet
- ◆ Calculators

- ◆ T will model how to multiply factorials (with proper notation) and how to use calculators to solve
- S will do worksheet on notation, writing out, and multiplying factorials
- ◆ T will go over multiplying factorials worksheet and assign homework

Dividing Factorials and Permutation Basics

- ◆ S will do Getting Started activity sheet
- ◆ T will model how to simplify fractional factorial expressions and create fractional factorial expressions (with and without calculator)
- S will do worksheet on notation, creating, writing out, and simplifying factorial expressions
- ◆ T will go over simplifying factorials worksheet
- ◆ T will introduce the definition of permutations, model the different formulas of a permutation, model how to use and write out a permutation
- ◆ S will do worksheet on the basics of permutations
- ◆ T will go over permutations worksheet and assign homework

Permutations with repetition

- ◆ S will do Getting Started activity sheet
- S will watch short video created by the Boston Red Sox over permutations
- ◆ T will model how to solve permutations with repetition (using proper notation), in reading problem form, and using calculators to solve
- ♦ S will do worksheets on notation, writing out, and solving permutations with repetition
- ◆ T will go over permutation worksheets and assign homework

Permutation without repetition

- ◆ S will do Getting Started activity sheet
- ◆ T will model how to solve permutations without repetition (using proper notation),,in reading problem form, and using calculators to solve
- ♦ S will do worksheets on notation, writing out, and solving permutations without repetition
- ◆ T will go over permutation worksheets and assign homework

Permutation (arranging problems)

- ◆ S will do Getting Started activity sheet
- ◆ T will refresh students on permutation definition and formulas
- S will use personal dry erase boards to compete in a game of permutations (to refresh on rules and how to solve)
- S will do worksheets on notation, writing out, and solving arranging problems (with and without repetition)
- ◆ T will go over arranging worksheets and assign homework

Combination Basics and Listing Combinations

- ◆ S will do Getting Started activity sheet
- ◆ T will introduce the definition of combinations, model the different formulas of a combination, and model how to use and write out a combination problem
- ◆ S will do worksheet on notation and writing out combinations
- ◆ T will go over combination worksheet
- ◆ T will model how to solve listing combinations (with and without calculators)
- S will do worksheet on listing combinations

- ◆ Getting Started problems
- Dividing factorials worksheet
- ♦ Basics of permutations worksheet
- Vocabulary sheet
- ♦ Calculators

- ♦ Getting Started problems
- Short video by Boston Red Sox on www.teachertube.com
- Permutations with repetition worksheets (numerical and word)
- ◆ Calculators
- Getting Started problems
- Permutations with repetition worksheets (numerical and word)
- ♦ Calculators
- Getting Started problems
- Personal dry erase boards
- Arranging (with and without repetition) worksheets
- Calculators
- Getting Started problems
- ◆ Basics of combinations worksheet
- ◆ Listing combinations worksheet
- ♦ Smartboard
- ♦ Vocabulary sheet
- ♦ Calculators

◆ T will go over listing combinations worksheet and assign homework

Combinations

- ◆ S will do Getting Started activity sheet
- ◆ T will model how to solve combination problems as repetitive permutations (numerical and word) with and without calculators
- S will do worksheet on combinations (numerical and word) using proper notation and with or without calculators
- ◆ T will go over combination worksheets and assign homework

Permutations/Combinations Which One?

- ◆ S will do Getting Started activity sheet
- ♦ S will use personal dry erase boards to compete over which problem is a combination or a permutation and then solve
- ◆ T will refresh over definitions, notation, and formulas used in permutations and combinations
- ♦ S will do worksheets on permutation/combination problems (finding out which one is which and writing the formulas used to solve)
- ◆ T will go over worksheets and assign homework

- Getting Started problems
- ◆ Combination worksheets
- ♦ Smartboard
- Calculators
- ◆ Getting Started problems
- Permutation/Combination worksheets
- Personal dry erase boards
- ♦ Smartboard
- ♦ Vocabulary sheets
- Calculators

Career Connections

Computer Programmer, Password designer, Restaurant owner, Clothing designer